

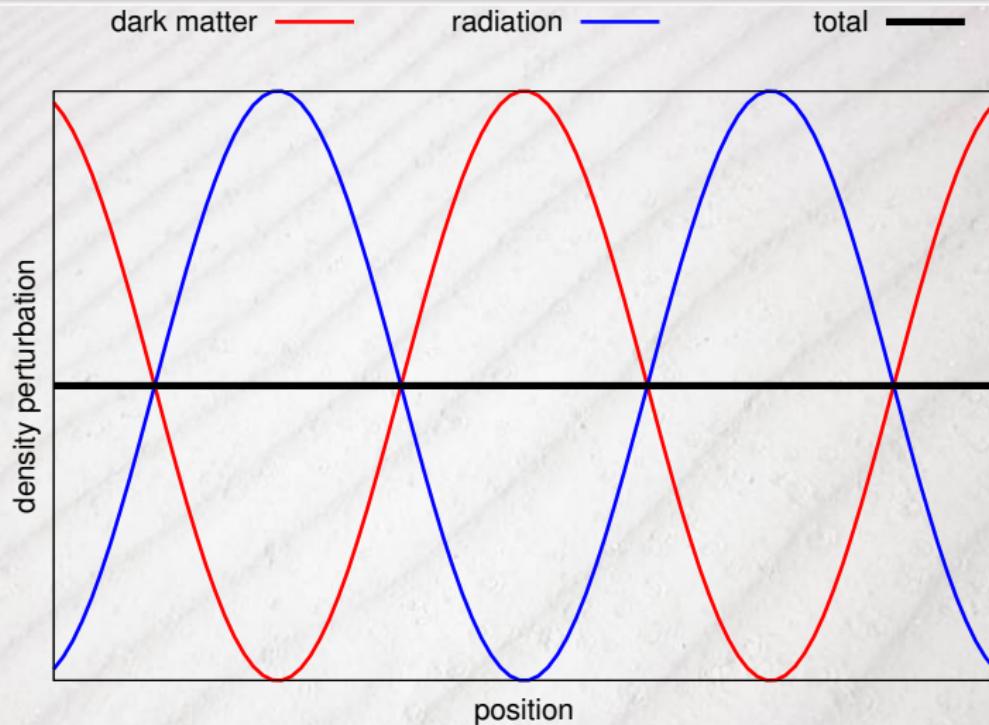
# **Cosmic surveys probe features in the inflationary power spectrum**

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June 20, 2017**

# Outline

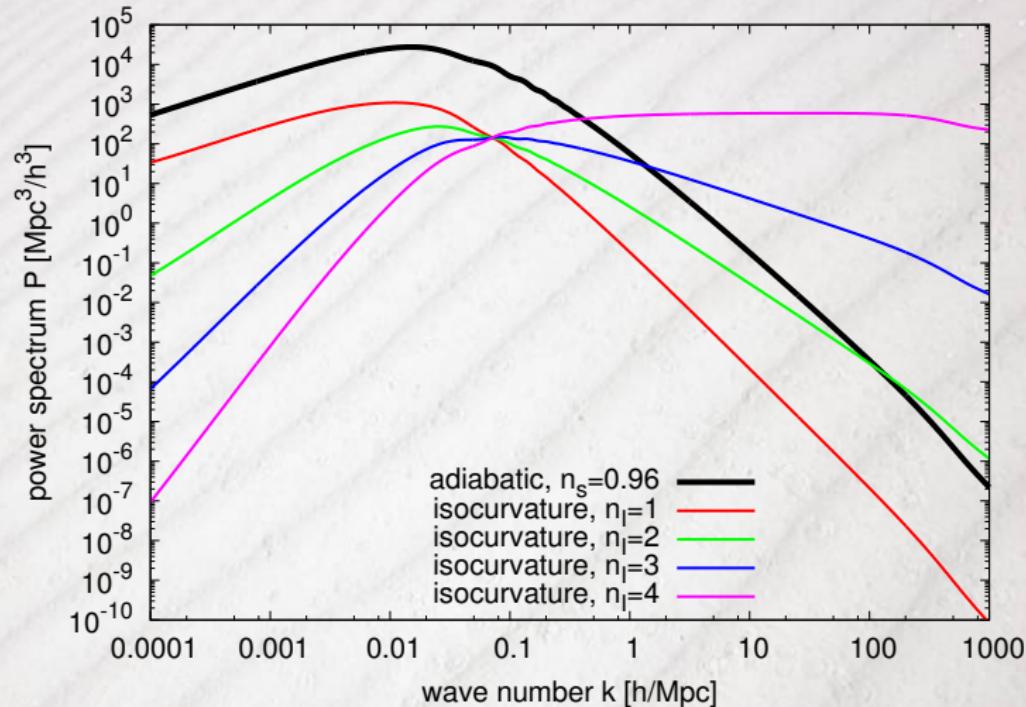
- Motivation: Inflation as a high-energy backlight illuminating new physics (fields and particles)
- Blue isocurvature: What and how
- A simple SUSY axionic model for blue isocurvature
  - Homogeneous field evolution
  - Perturbations and power spectra
- Large-scale cosmic structure is complementary to CMB

# Isocurvature



We expect isocurvature perturbations when additional fields are non-negligible during inflation.

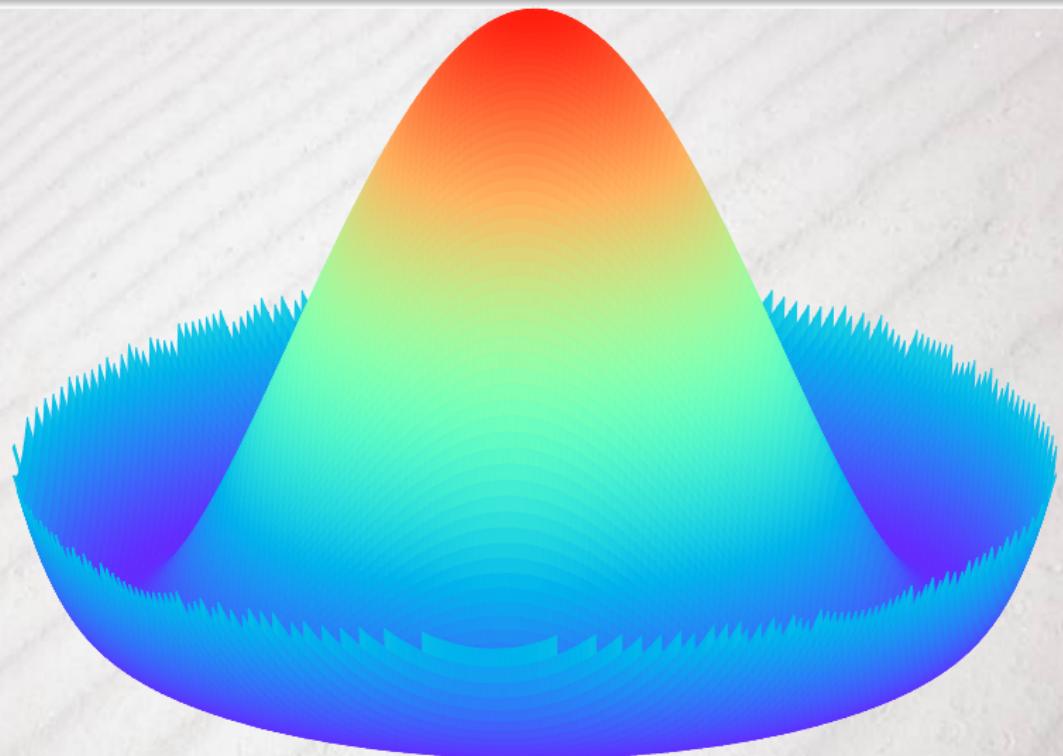
# Isocurvature can't be blue at all scales



Isocurvature with a constant spectral index can't be bluer than  $n_I = 2.4$ .

Chung, PRD 94:043524(2016)[1509.05850]

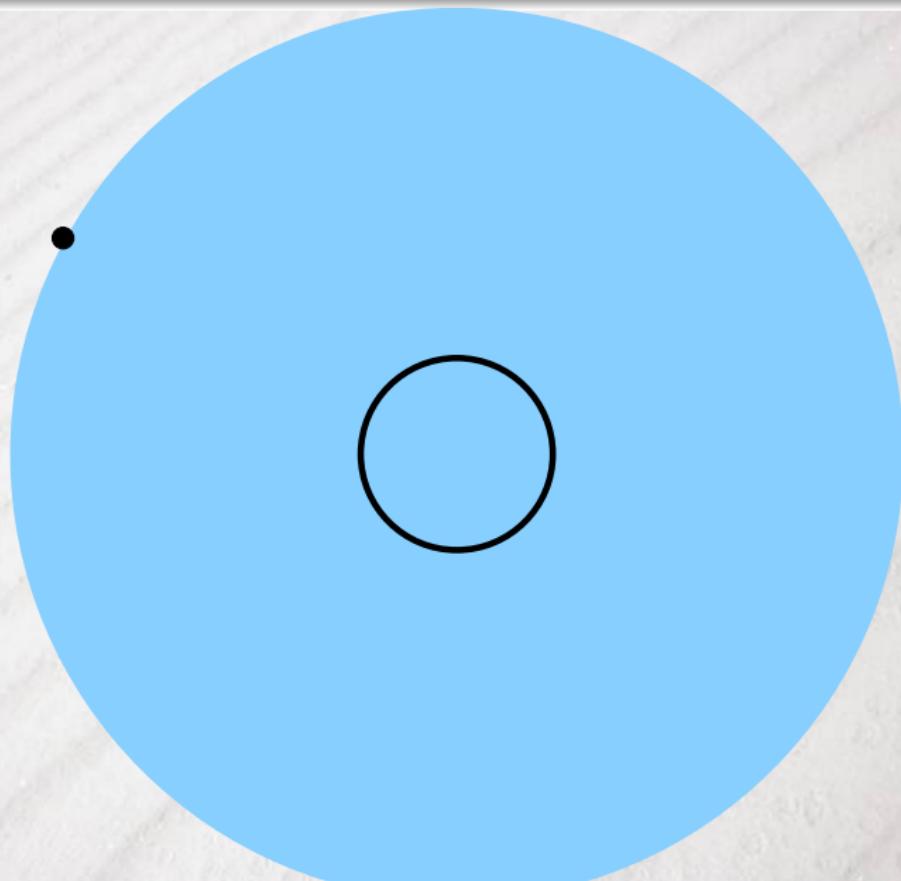
# Blue spectrum from axionic field



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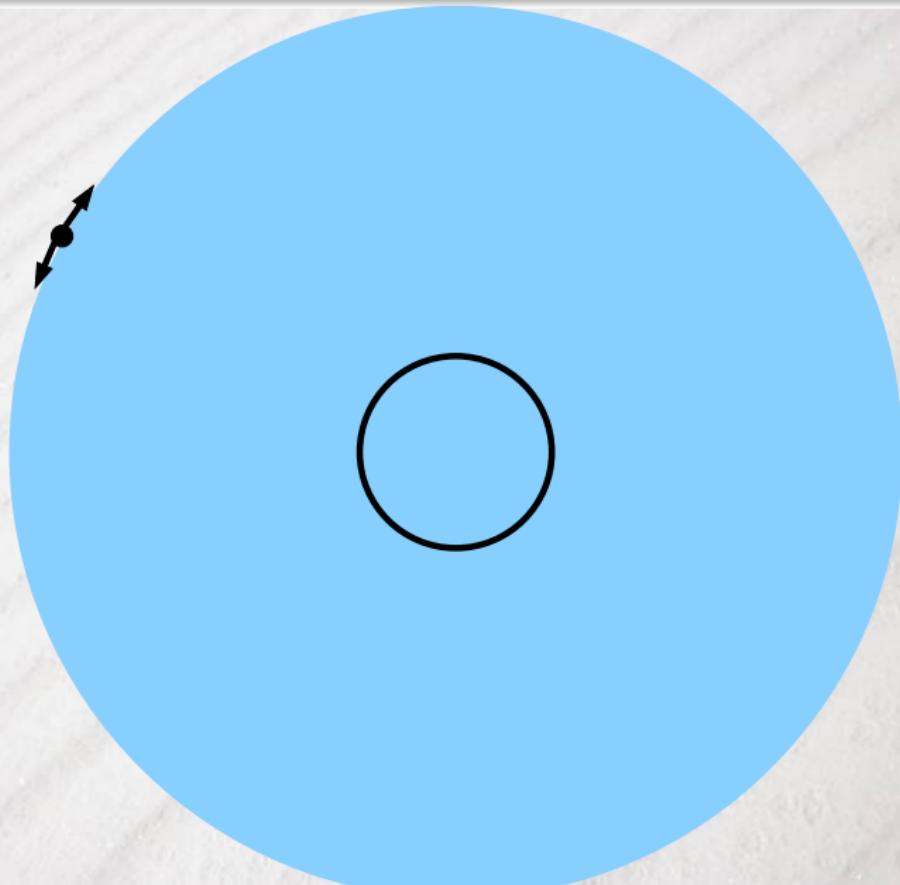
“Hat” potential  $V(\Phi) = (\Phi^2 - F_a^2)^2$

# Blue spectrum from axionic field



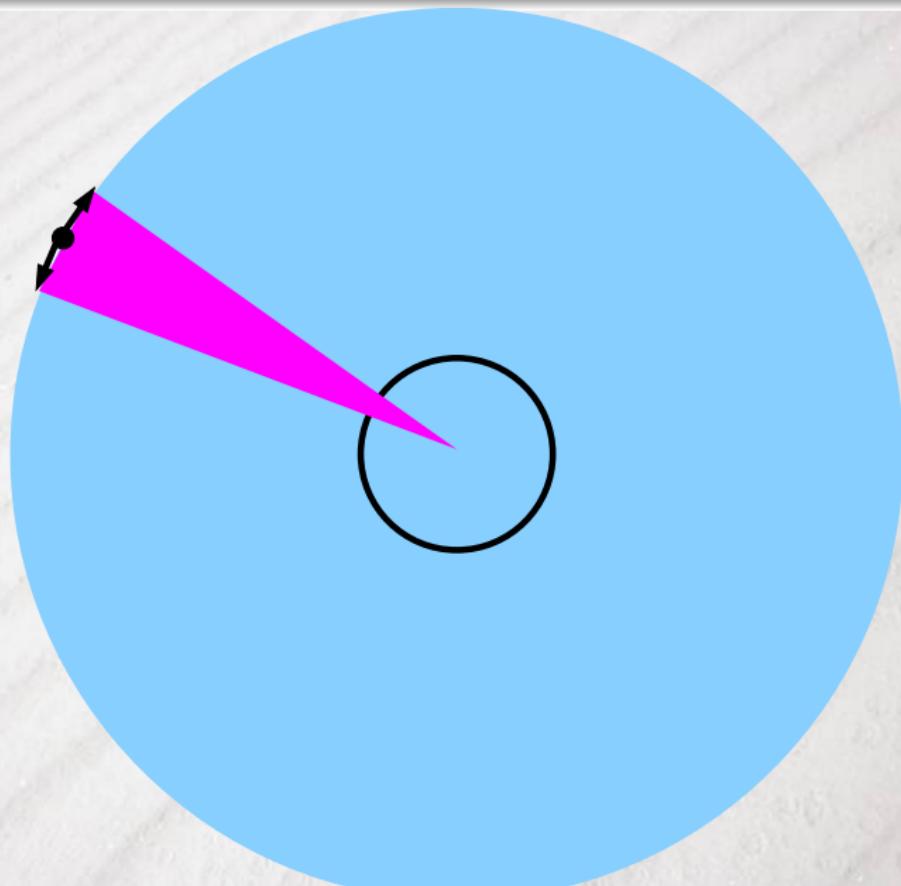
(out-of-equilibrium axion mass term  $\frac{\Box f_{\text{PQ}}}{f_{\text{PQ}}} a^2 \sim H^2 a^2$ )

# Blue spectrum from axionic field



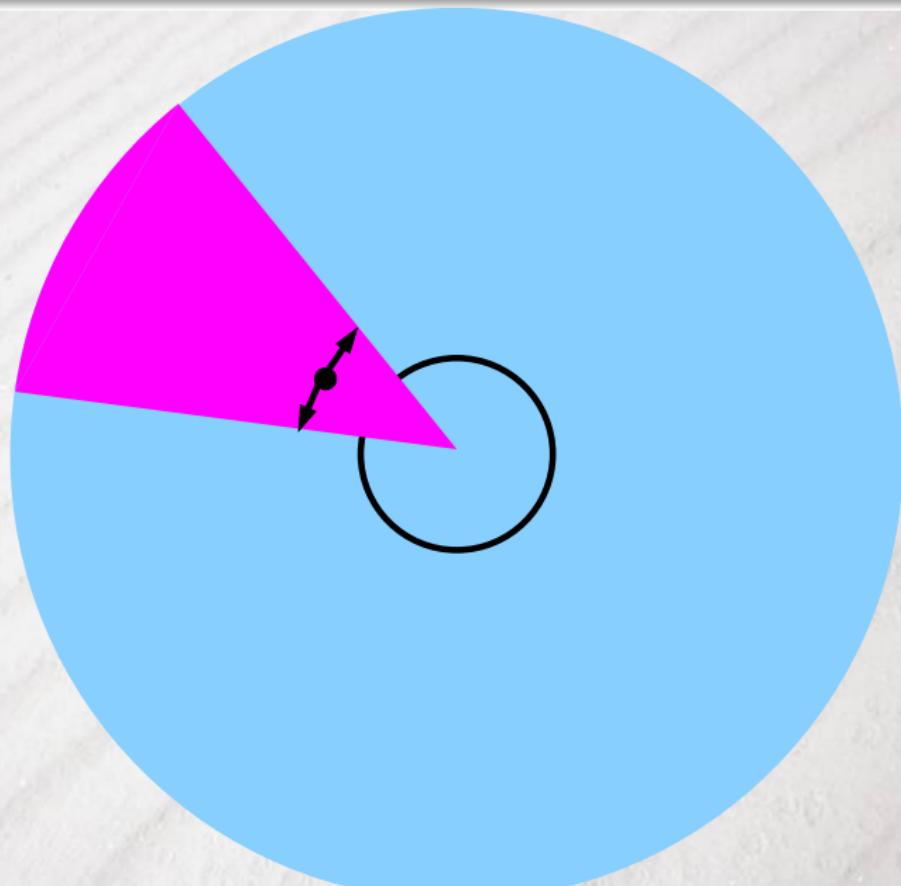
(out-of-equilibrium axion mass term  $\frac{\Box f_{\text{PQ}}}{f_{\text{PQ}}} a^2 \sim H^2 a^2$ )

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# Blue spectrum from axionic field



(out-of-equilibrium axion mass term  $\frac{\Box f_{\text{PQ}}}{f_{\text{PQ}}} a^2 \sim H^2 a^2$ )

# Supersymmetric axion model

Superpotential  $W = h(\Phi_+ \Phi_- - F_a^2)\Phi_0$  for chiral superfields with charges +1, -1, and 0 under  $U(1)$  Peccei-Quinn symmetry

$$\Rightarrow V = h^2 |\Phi_+ \Phi_- - F_a^2|^2 + h^2 |\Phi_0|^2 (|\Phi_+|^2 + |\Phi_-|^2)$$

Flat direction:  $\Phi_0 = 0$ ,  $\Phi_+ \Phi_- = F^2$ .

Potential along the flat direction, including Hubble-scale mass corrections (from Kähler potential):

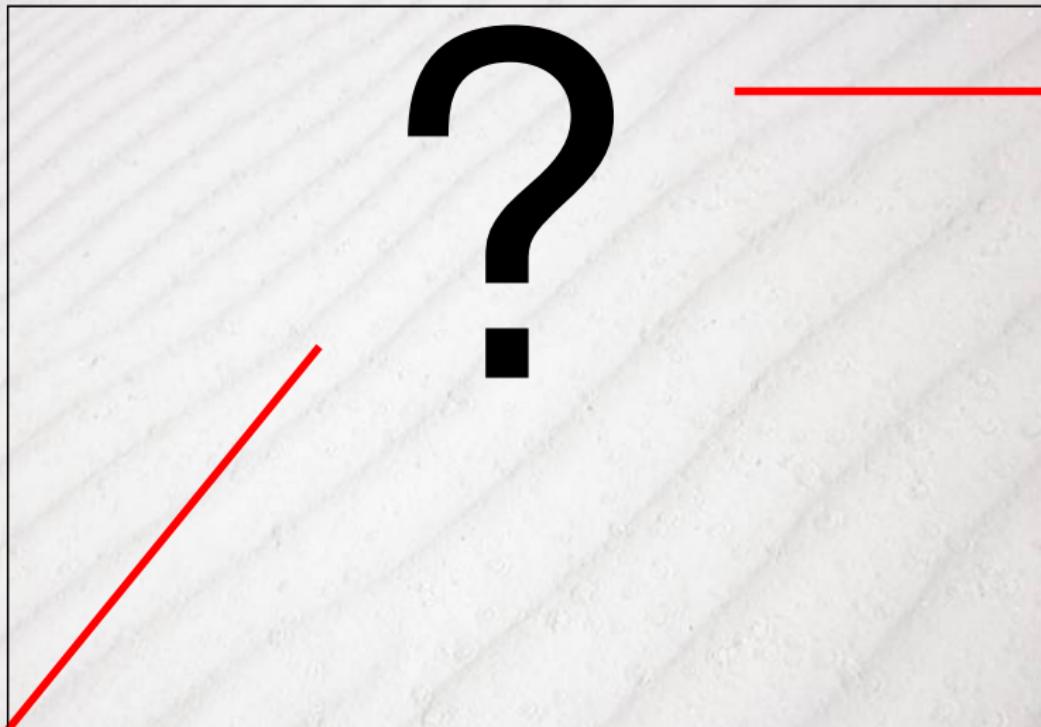
$$V = h^2 |\Phi_+ \Phi_- - F_a^2|^2 + c_+ H^2 |\Phi_+|^2 + c_- H^2 |\Phi_-|^2$$

- “roll speed”  $\gamma = \frac{3}{2} \left( 1 - \sqrt{1 - \frac{4}{9} c_+} \right)$  with  $\Phi_+ \propto \exp(-\gamma H t)$ ;
- spectral index  $n_I = 1 + 2\gamma = 4 - 3\sqrt{1 - \frac{4}{9} c_+}$
- blue e-folds:  $\eta_* = \gamma^{-1} \log \left( \frac{\Phi_{+,in}}{F_a} \frac{c_+^{1/4}}{c_-^{1/4}} \right)$

Kasuya and Kawasaki, PRD 80:023516(2009)[0904.3800],

Chung and Yoo, PRD 91:083530(2015)[1501.05618]

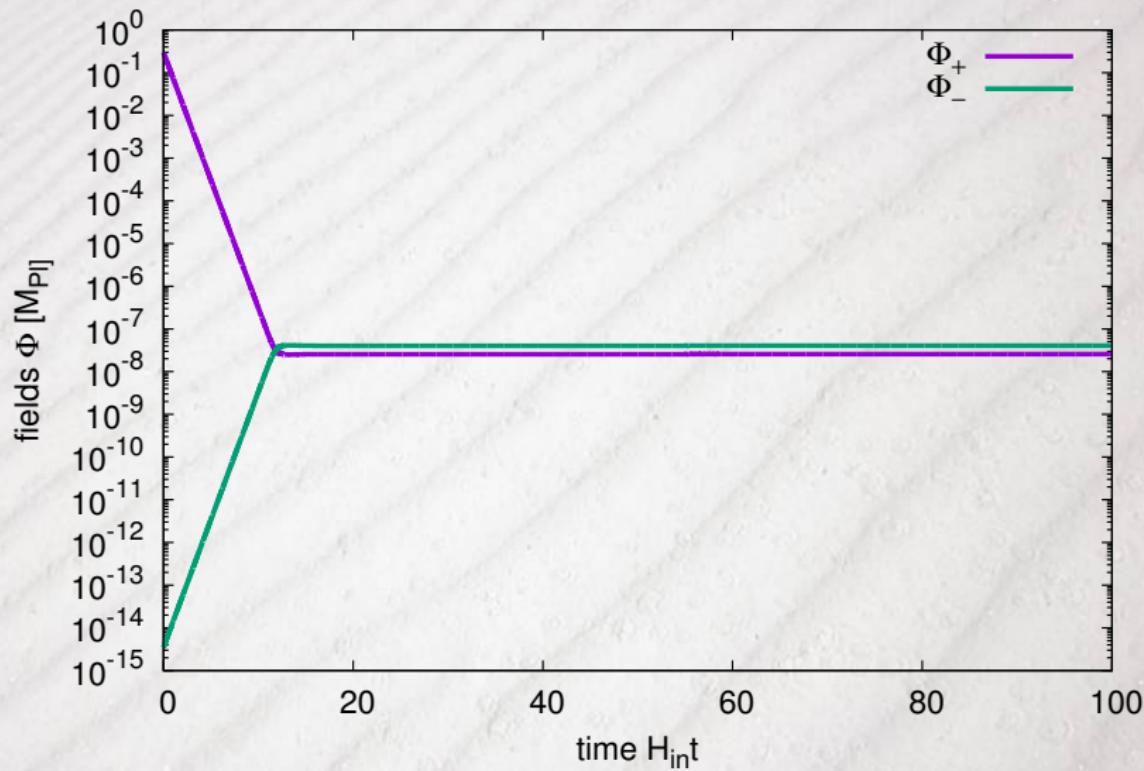
# Power spectrum from analytic arguments



Kasuya and Kawasaki, PRD **80**:023516(2009)[0904.3800],

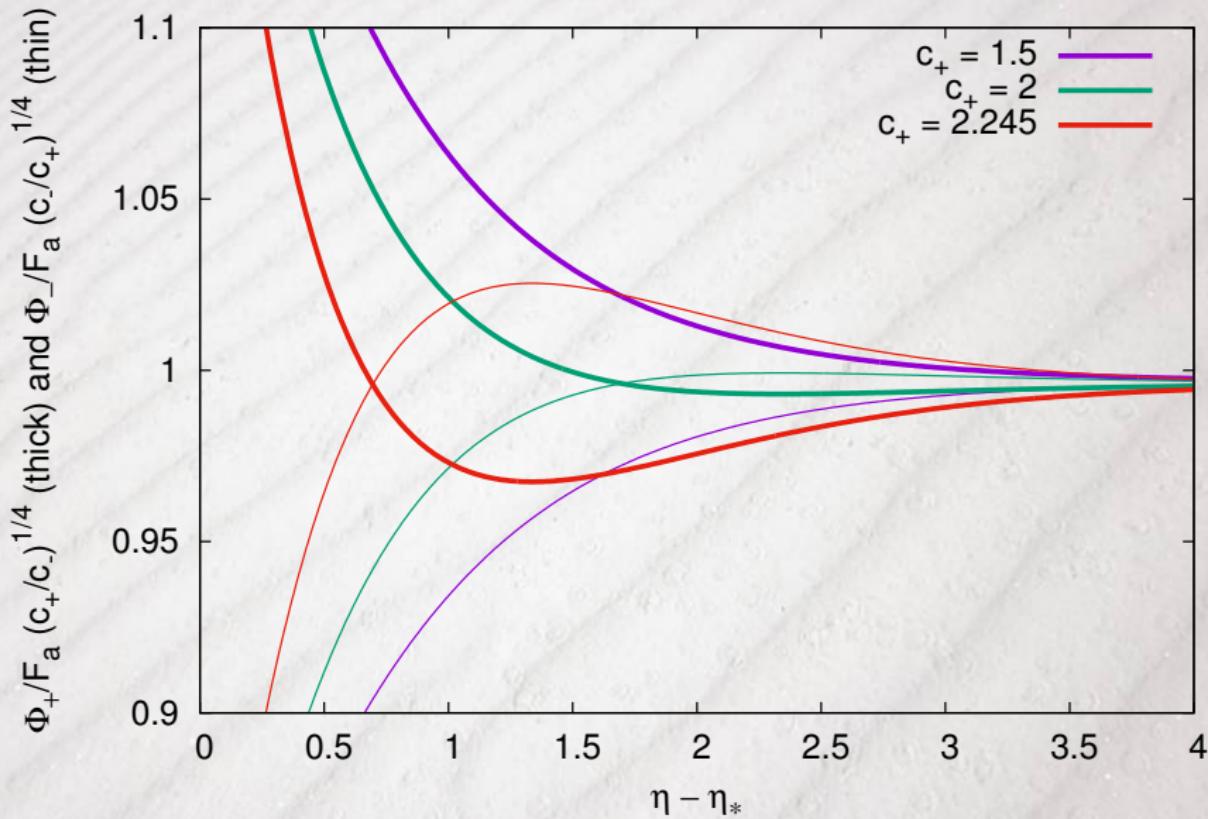
Chung and Yoo, PRD **91**:083530(2015)[1501.05618]

# Field evolution in homogeneous universe

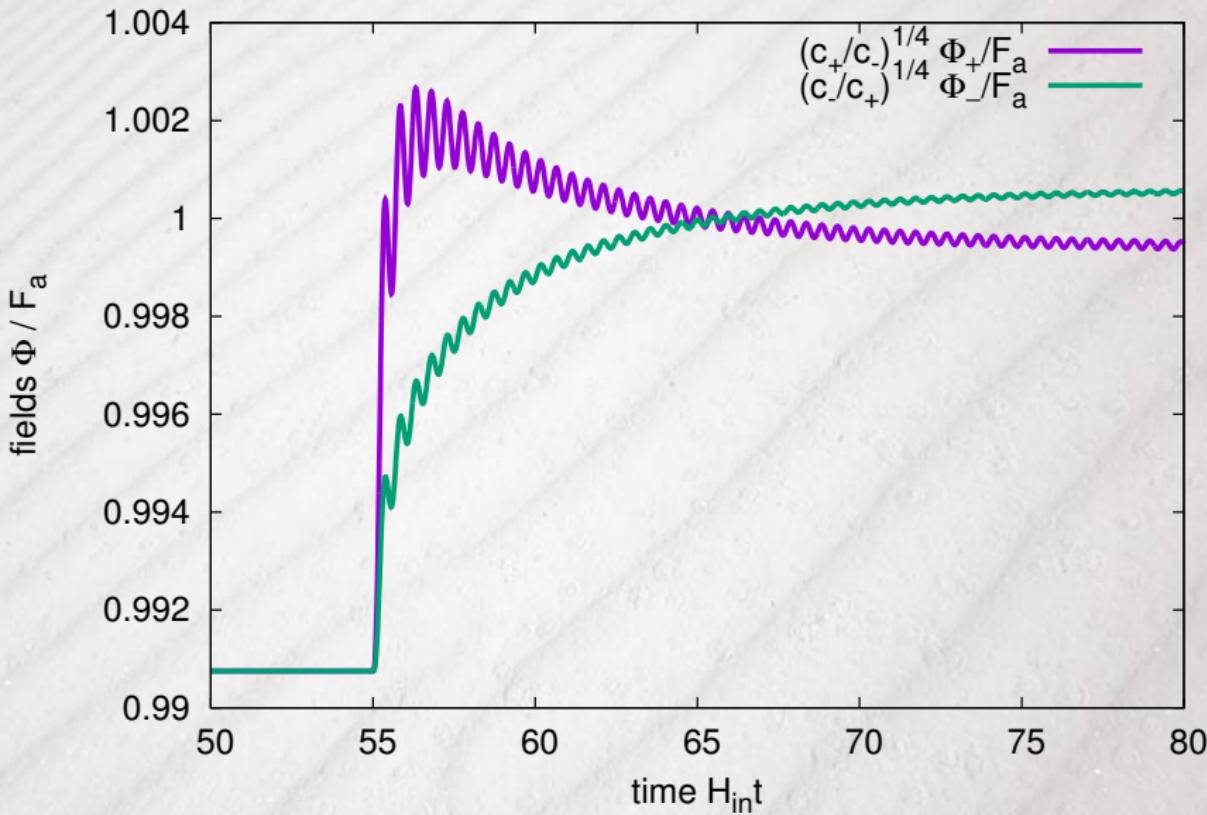


Chung and Upadhye, PRD 95:023503(2017)[1610.04284]

# Blue-to-flat transition



# End of inflation



# Evolution of linear perturbations

Perturbations  $R_{\pm} = \text{Re}(\delta\Phi_{\pm})$  and  $I_{\pm} = \text{Im}(\delta\Phi_{\pm})$  are evolved using

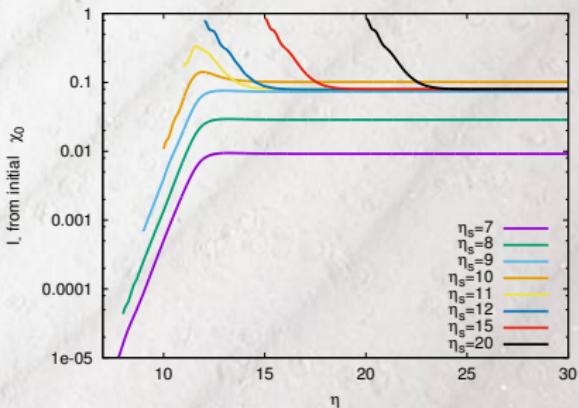
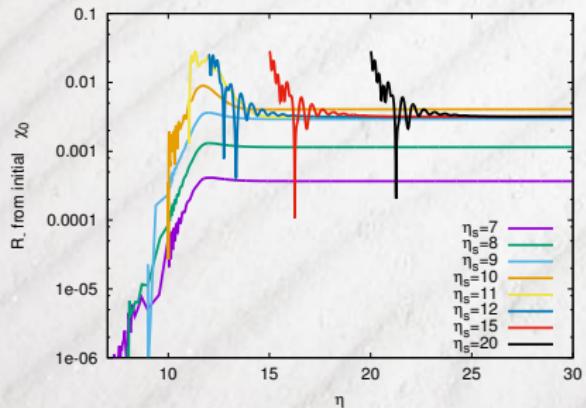
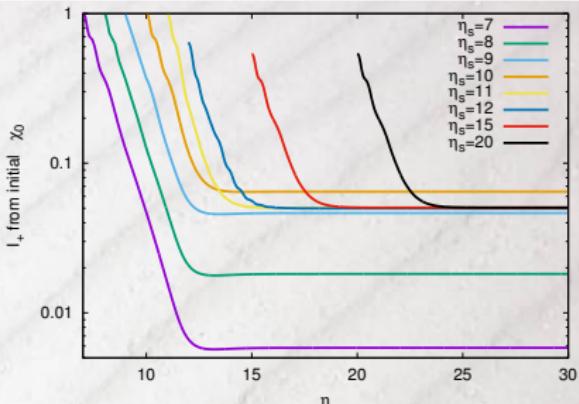
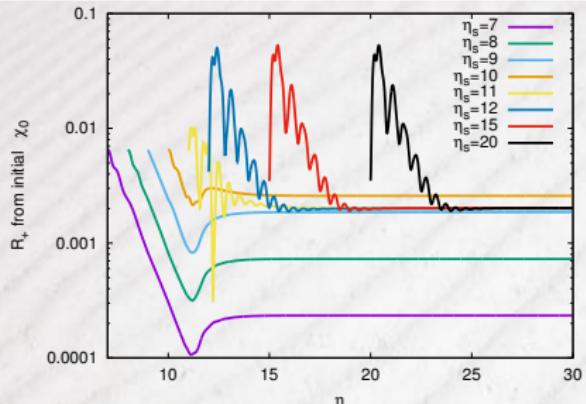
$$\begin{aligned}\ddot{R}_+ + 3H\dot{R}_+ + \left(c_+ H^2 + \frac{k^2}{a^2} + h^2 \Phi_-^2\right) R_+ = \\ -h^2(\Phi_+ \Phi_- - F_a^2) R_- - h^2[\cos(2\theta_+) R_- - \sin(2\theta_+) I_-] \Phi_+ \Phi_-\end{aligned}$$

$$\begin{aligned}\ddot{I}_+ + 3H\dot{I}_+ + \left(c_+ H^2 + \frac{k^2}{a^2} + h^2 \Phi_-^2\right) I_+ = \\ h^2(\Phi_+ \Phi_- - F_a^2) I_- - h^2[\cos(2\theta_+) I_- + \sin(2\theta_+) R_-] \Phi_+ \Phi_-\end{aligned}$$

$$\begin{aligned}\ddot{R}_- + 3H\dot{R}_- + \left(c_- H^2 + \frac{k^2}{a^2} + h^2 \Phi_+^2\right) R_- = \\ -h^2(\Phi_+ \Phi_- - F_a^2) R_+ - h^2[\cos(2\theta_+) R_+ + \sin(2\theta_+) I_+] \Phi_+ \Phi_-\end{aligned}$$

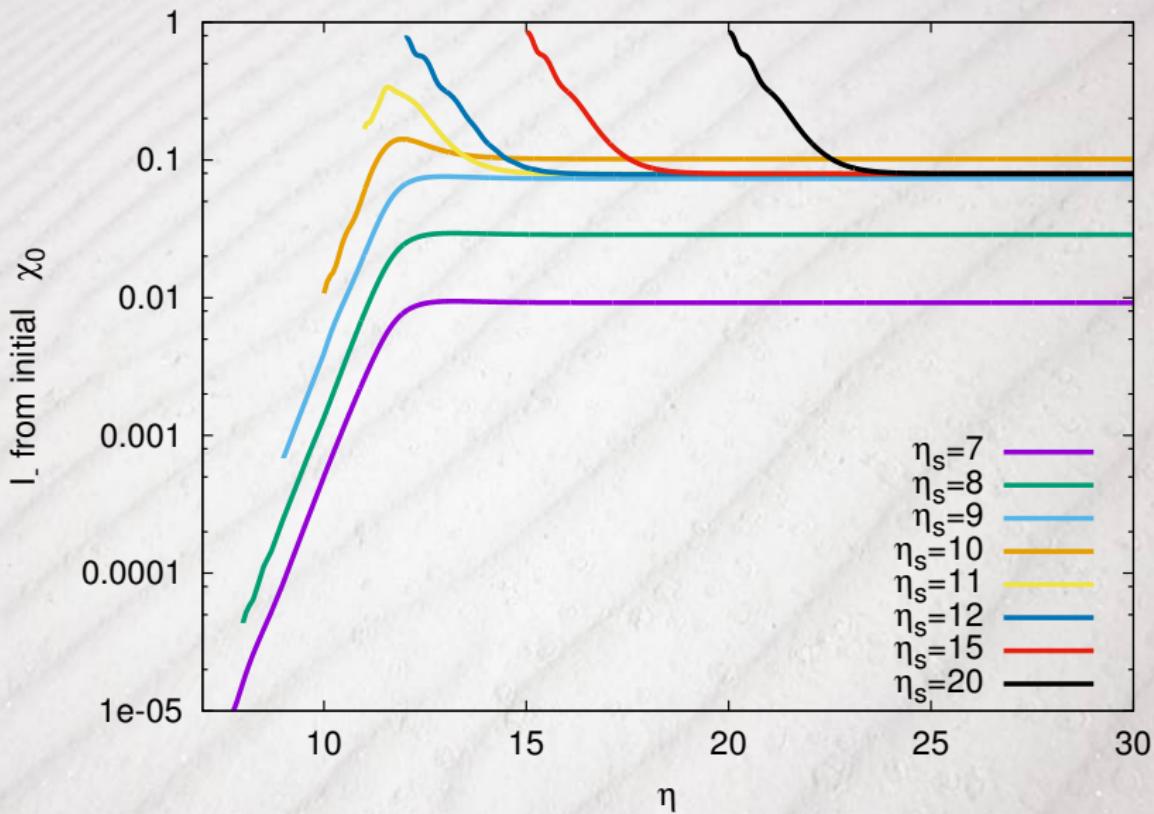
$$\begin{aligned}\ddot{I}_- + 3H\dot{I}_- + \left(c_- H^2 + \frac{k^2}{a^2} + h^2 \Phi_+^2\right) I_- = \\ h^2(\Phi_+ \Phi_- - F_a^2) I_+ - h^2[\cos(2\theta_+) I_+ - \sin(2\theta_+) R_+] \Phi_+ \Phi_-\end{aligned}$$

# Evolution of linear perturbations



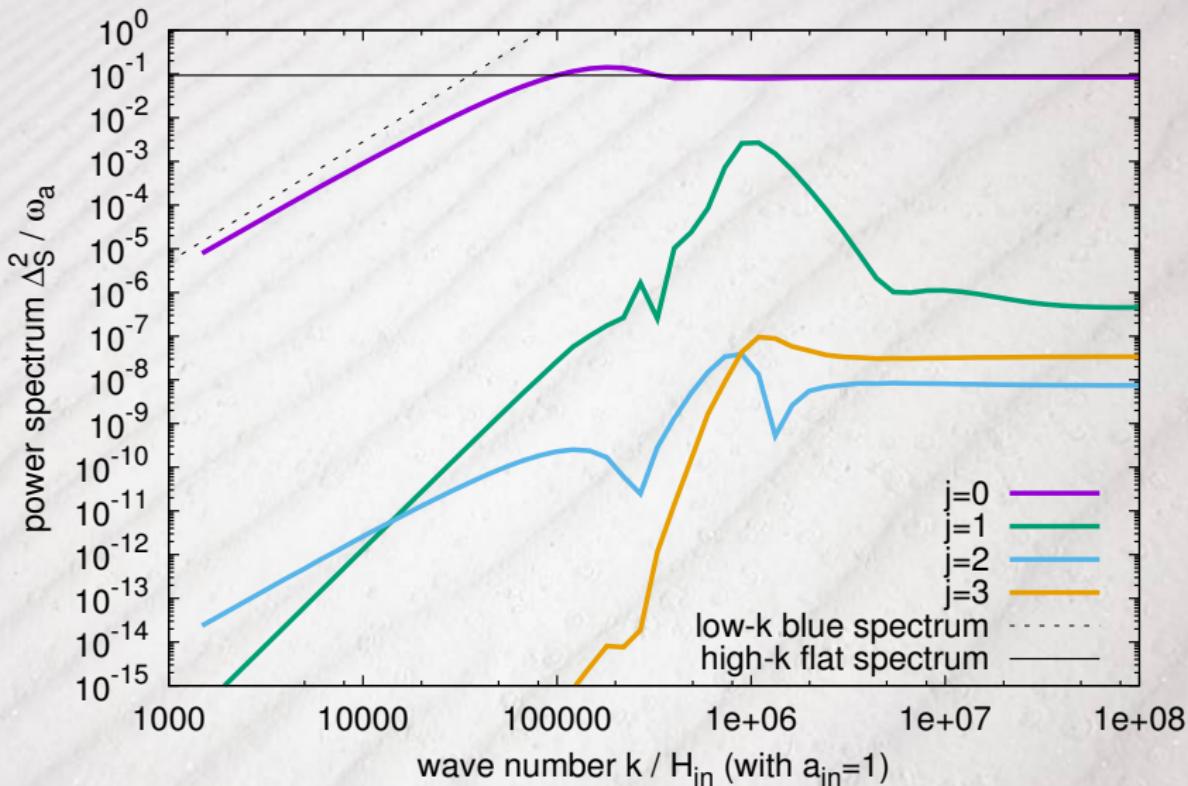
Chung and Upadhye, PRD 95:023503(2017)[1610.04284]

# Evolution of linear perturbations



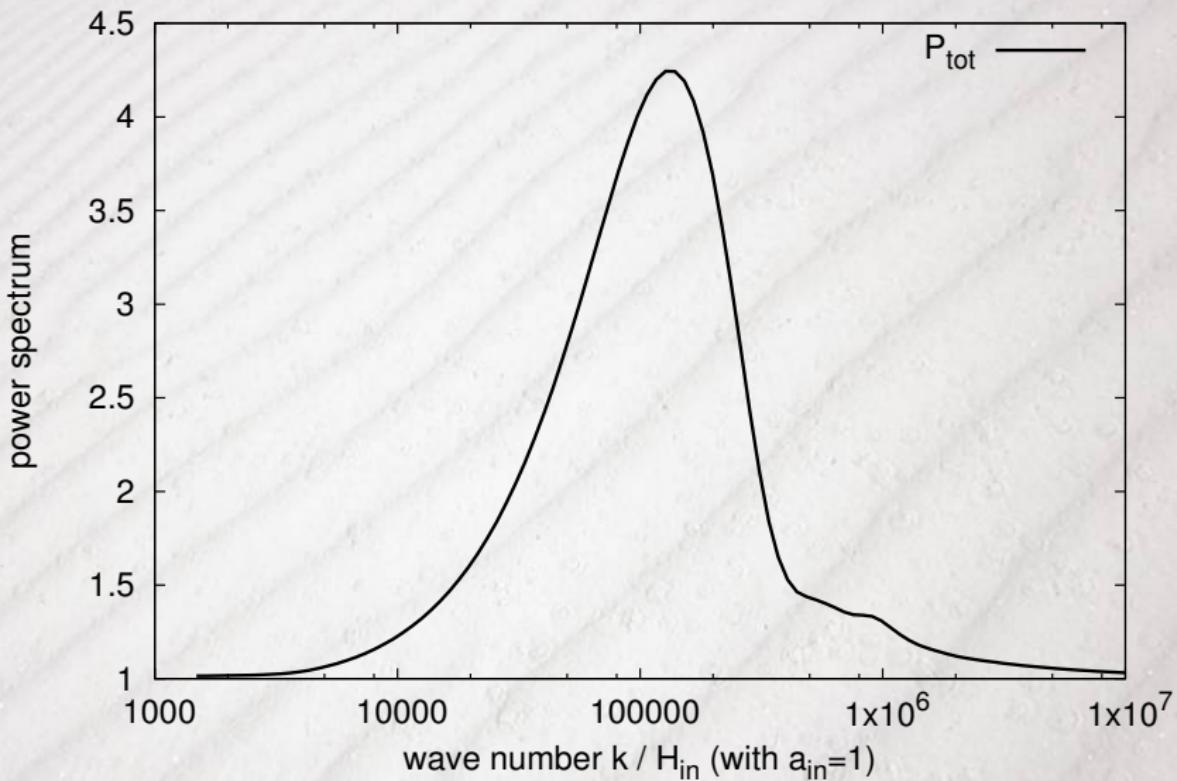
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# Power spectrum, $c_+ = 2.235$



Chung and Upadhye, PRD 95:023503(2017)[1610.04284]

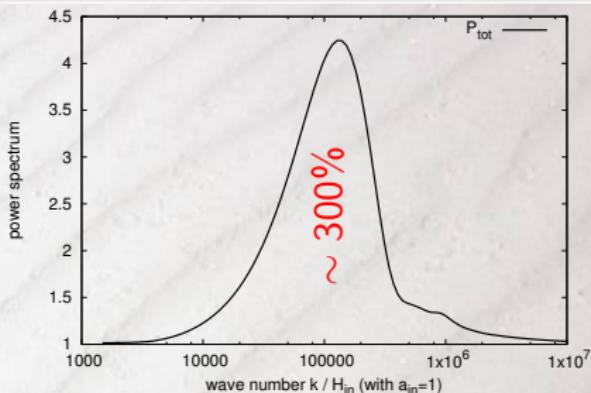
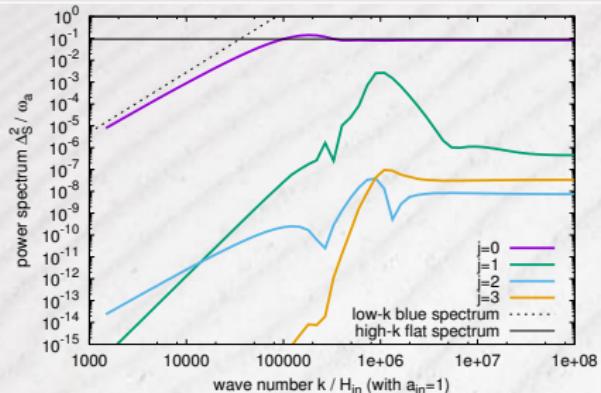
# Power spectrum, $c_+ = 2.235$



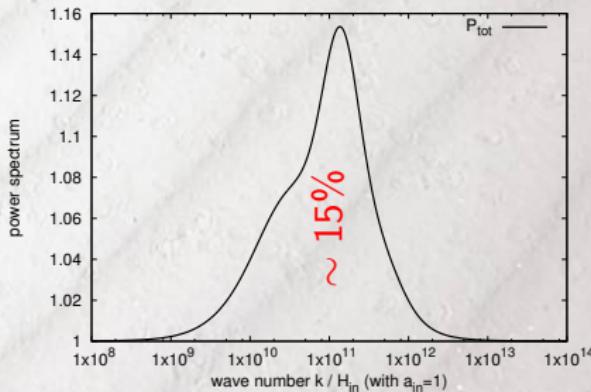
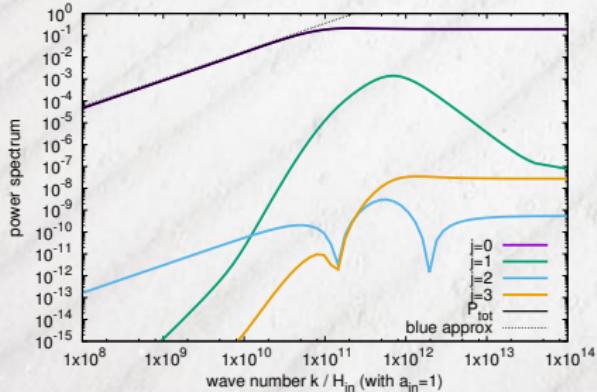
Chung and Upadhye, PRD 95:023503(2017)[1610.04284]

# Bluer spectra get bigger bumps

$$c_+ = 2.235$$

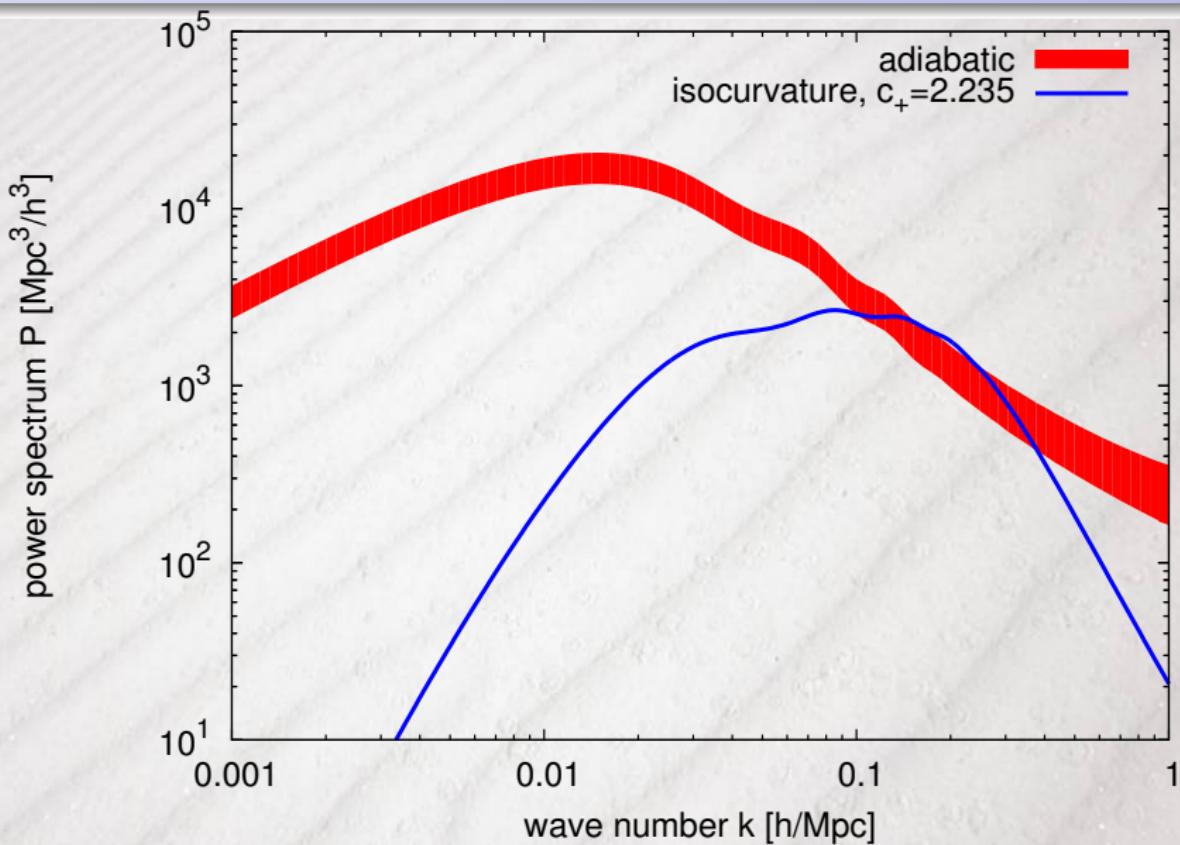


$$c_+ = 1.5$$



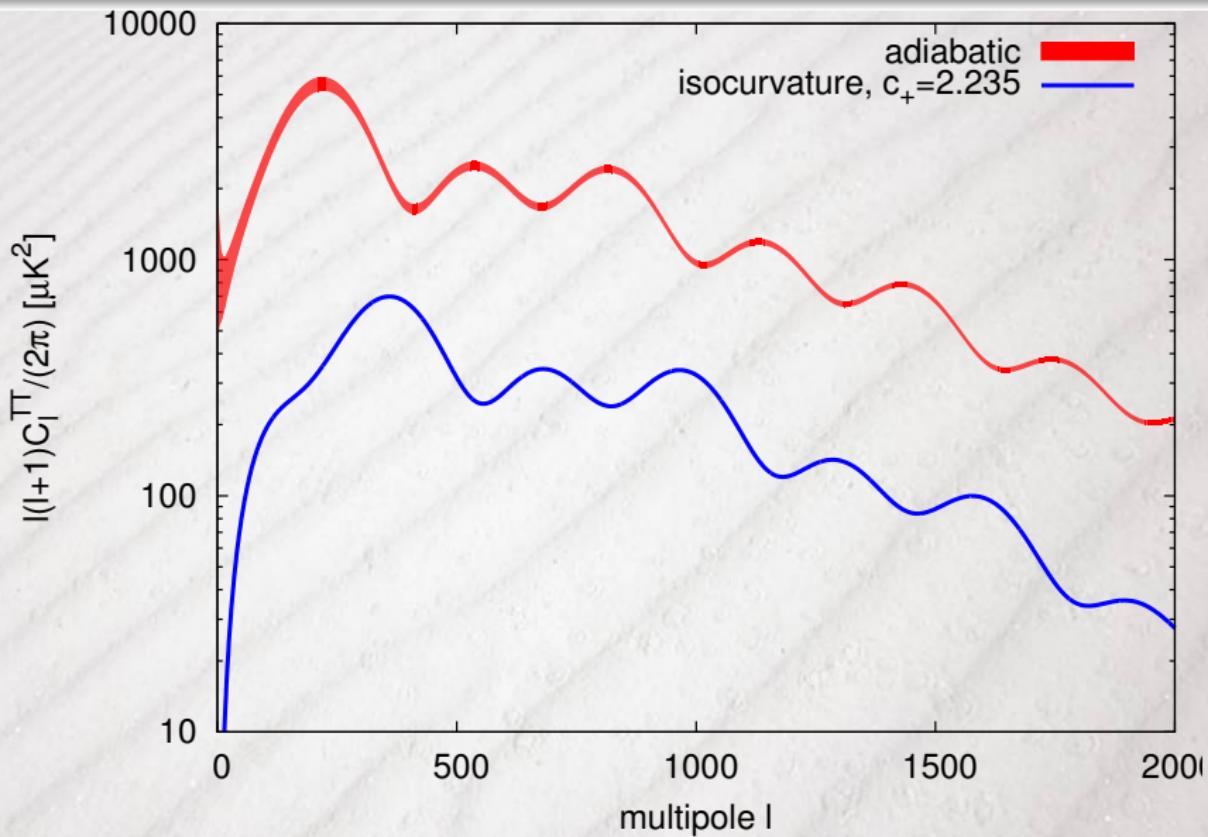
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# Cosmic structure constrains models invisible to the CMB



Upadhye and Chung (2017, in prep.)

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# Conclusions

- ➊ Cosmic inflation can serve as a backlight illuminating other physics at high energies.
- ➋ Additional fields during inflation will acquire isocurvature perturbations,  $P_I(k) = A_I k^{n_I}$ . The bluest models must transition to flatter spectra.
- ➌ A simple SUSY axion model can have very blue spectra  $2.4 < n_I < 4$  inaccessible to constant-mass models.
- ➍ Power spectra for the bluest models have a characteristic bump at the transition scale that can be used to search for them in current and near-future large-scale structure surveys.
- ➎ For QCD axion candidates, this transition cannot be pushed beyond  $k_* = 10 - 20 h/\text{Mpc}$  for the bluest tilts.